

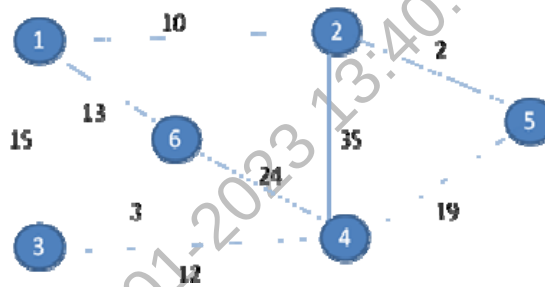
B. TECH.
(SEM V) THEORY EXAMINATION 2022-23
DESIGN & ANALYSIS OF ALGORITHM

Time: 3 Hours**Total Marks: 70****Note:** Attempt all Sections. If require any missing data; then choose suitably.**SECTION A****1. Attempt all questions in brief.****2 x 7 = 14**

- (a) Explain the different cases for analyzing the algorithm performance.
- (b) Justify why Quick sort is better than merge sort?
- (c) What is the maximum height of red-black tree with 10, 00,000 nodes?
- (d) Explain Binomial tree with properties.
- (e) Explain Backtracking method in brief.
- (f) Discuss P, NP and NP-hard problem.
- (g) Write naïve string matching algorithm.

SECTION B**2. Attempt any three of the following:****7 x 3 = 21**

- (a) Solve the following recurrence relation
 - i. $T(n) = T(n-1) + n^4$
 - ii. $T(n) = 2T(n/2) + n$
- (b) Write and explain an algorithm for Decrease key operation in Fibonacci heap with suitable example.
- (c) Write Kruskal algorithm to generate a Minimum Spanning Tree (MST) for any given weighted graph. Generate MST for the following graph using Kruskal algorithm.



- (d) Write down Floyd Warshal algorithm and also write its time complexity.
- (e) Explain randomized algorithm. Write randomized quick sort algorithm.

SECTION C**3. Attempt any one part of the following:****7 x 1 = 7**

- (a) Sort the following elements in increasing order, using **quick sort** { 14, 23, 41, 35, 67, 9, 40, 16, 9, 12 }
- (b) Write merge sort algorithm and analyze its time complexity in all cases.

4. Attempt any *one* part of the following: 7 x 1 = 7
- (a) Write down Red Black tree properties also write algorithm for insertion in RB tree.
 - (b) Write and explain an algorithm to find a node with minimum key value in Binomial Heaps and also write its time complexity.
5. Attempt any *one* part of the following: 7 x 1 = 7
- (a) Compare the dynamic programming with greedy approach.
 - (b) Discuss Bellman Ford algorithm to solve single source shortest path problem.
6. Attempt any *one* part of the following: 7 x 1 = 7
- (a) What is knapsack problem? Discuss the branch & bound method to solve 0/1 knapsack problem. Given Knapsack Capacity=12.
- | | | | | |
|--------|----|----|----|----|
| Weight | 5 | 7 | 4 | 2 |
| Profit | 30 | 28 | 20 | 24 |
- (b) Write an algorithm for graph coloring problem. Draw a state space tree for graph coloring problem using backtracking? Let **n=4** and **m=3**.
7. Attempt any *one* part of the following: 7 x 1 = 7
- (a) Write KMP algorithm for string matching? Compute the prefix function for the pattern “ababababca” for the alphabet set {a, b, c} and also write its time complexity.
 - (b) Define vertex cover. What is vertex cover problem? Provide the approximation algorithm for vertex cover problem.